

- 1) Name
- 2) taking AP?
- 3) turned in form
- 4) which exam & why?
- 5) 3-4 topics that concern you the most

True or False?

If False, find a function that shows it

If true, give me the sketch of an argument

- 1.1) The tangent to a curve at a point is the line that touches the curve at that point, but does not cross it there.
- 1.2) The tangent line to a curve at a point cannot touch the curve at infinitely many other points.
- 2.1) If  $f(x) < g(x)$  for all  $x > 0$ , and both  $\lim_{x \rightarrow \infty} f(x)$  and  $\lim_{x \rightarrow \infty} g(x)$  exists, then  $\lim_{x \rightarrow \infty} f(x) < \lim_{x \rightarrow \infty} g(x)$

aaa

8.8/6

$$\int_0^{\infty} x e^{-x^2} dx = \lim_{b \rightarrow \infty} \int_0^b x e^{-x^2} dx$$

Let  $u = x^2$

$$\frac{du}{dx} = \frac{2x}{1} \Rightarrow \frac{du}{2} = x dx$$

$$\frac{1}{2} du = x dx$$

$$\int \frac{1}{2} e^u du$$

$$= \frac{1}{2} e^u + C \Rightarrow \frac{1}{2} e^{x^2} + C \rightarrow \lim_{b \rightarrow \infty} \frac{1}{2} e^{x^2} \Big|_0^b$$

$$= \lim_{b \rightarrow \infty} \left[ \frac{1}{2} e^{b^2} - \left( \frac{1}{2} e^0 \right) \right]$$

$$= \lim_{b \rightarrow \infty} \frac{1}{2} e^{b^2} + \frac{1}{2} = \frac{1}{2}$$